Introduction—State of the Art

Large, high-speed load gears are predominantly manufactured with case-hardened, double helical teeth and supported by plain bearings in welded steel gear casings. Since gear widths can become very large at these power transmissions levels, double helical gears have come to predominate over single helical gears, because:

- The face width is divided into two tooth halves.
- No free axial forces result from the helix angle of the teeth.
- A considerably larger helix angle can be used (25–30° compared to 10–15°) to give a high face contact ratio and an improvement in acoustic behavior.
- Bearing forces are symmetrical with no tilting moment.

(Single helical gearing has a tilting moment, which is the result of the helix-angle-produced thrust force acting at the pitch diameter.)

- No thrust bearing is required on the pinion and gear wheel—only a guide bearing is needed on the wheel set, and this can be located on the shaft with the lowest speed.

In terms of materials, the case hardening grade 18CrNiMo7–6 (former designation 17CrNiMo6) is almost universal. The wheel set is designed as a single piece due to the high tip speed of $\geq 150$ m/sec., i.e., wheel and shaft are a single forging and as a matter of principle the pinion is cut from a single piece of material.

Shaft support takes the form of offset or tilting-pad bearings.

Failure Mechanisms

Typical failures on the gear wheel are tooth breakage and damage to the tooth flanks. Tooth breakages can be impact fractures or fatigue fractures. Tooth flank damage is a symptom of wear and can lead to fatigue fractures. The types of failure are shown in Figure 1.

Figure 1 includes erosion as a surface disturbance failure mode. Erosion is material removal associated with liquid impingement from oil jets in high-speed gearing. Erosion can be avoided by using special nozzles with a soft oil-jet flow to spray the gear mesh.

Since the subject transmissions have very high tip speeds, which promote the build-up of a good film of lubricant on the gear flanks, they are relatively insensitive to pitting and micro-pitting. Preconditions for the avoidance of these failure modes are, of course, the use of the correct lubricant and the surface condition (roughness) of the tooth flanks.

In the experience of the authors, in the subject transmissions, special attention must be paid to freedom from cracking (friction cracks) and adequate resistance to erosion and flank fractures.

The flank fracture is shown in Figure 2 as a micro section. It originates within the material, predominantly at non-metallic inclusions below the hardened layer and/or in the transition from the hardened exterior to the non-hardened parent metal. The path of the fracture is inclined at 45° to the flank with its point of emergence approximately at the pitch circle. Fractures principally occur in areas of high load concentration. Such areas can result in the shaft during operation under unfavorable stress conditions. Unfavorable stress conditions are thermal stresses in the rotor due, for example, to cold start-ups or uneven temperature distribution over the width of the teeth.

Ideas and Recommendations—Methods of Computation

As a matter of principle, the gear tooth design should be computed for:

- Tooth-bending strength.
- Surface durability (pitting).
- Scuffing.

Methods for calculation of the prevention of tooth bending and flank pressure are dealt with at length in AGMA 421.06, API 613 and ISO 13691. AGMA 421.06 was replaced by ANSI/AGMA 6011–G92, and this was again refined by ANSI/AGMA 6011–H98. As regards API 613, in this
paper we address API 613 Fifth Edition 2003. Although it is an American national standard, it is applied worldwide. This is the case since there is no standard like DIN 3990 or ISO 6336 exclusively concerned with the computation of gear teeth, but also containing complete design instructions for the transmission, based on experience and failure statistics of machines operating in the field. Modeled closely on API 613 Fifth Edition, the ISO 13691 standard has emerged as an international standard.

For the design of gear teeth, ISO 6336 Parts 1–5 serve as a basis, whereby careful attention must be paid to the fact that transmission size is identical according to both API and ISO. In this way, the API Service Factor also corresponds to the Selection Factor of ISO 13691. In the meantime, since February 2003 there has existed API 613 Fifth Edition, which, conversely, has taken over various aspects from ISO 13691. It thus has a more international character but remains nonetheless a national norm. It is regrettable that both standards compete with each other instead of ISO and API working together to produce an international standard on the subject. The disadvantage of a national standard is that for different countries (i.e., outside the United States), various deviations have to be discussed and accepted during contract negotiations.

For the calculation of scuffing, there are the integral-temperature and the flash-temperature methods, which are dealt with in the Technical Reports ISO/TR 13989-2 and ISO/TR 13989-1. No particular procedure is favored, but the suggestion is to use the procedure with which the transmission builder is most experienced.

**Tooth Corrections**

To achieve the most even load distribution possible, corrections are necessary in the direction of tooth height and tooth width. In the direction of height, the correction on the tip of the tooth of the driving gear serves to attenuate meshing impact.

In the lateral direction, the cor-
Table 1—Mechanical Properties

<table>
<thead>
<tr>
<th>Material Class</th>
<th>Rm (MPa)</th>
<th>Re (MPa)</th>
<th>A (%)</th>
<th>KCU (J/cm²)</th>
<th>K1C (MPa m½)</th>
<th>∆HRC</th>
<th>Tempering (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>18CrNiMo7-6</td>
<td>1400</td>
<td>1040</td>
<td>13</td>
<td>85</td>
<td>78</td>
<td>&gt; 9</td>
<td>150 / 180</td>
</tr>
<tr>
<td>16NiCrMo13</td>
<td>1380</td>
<td>1100</td>
<td>13</td>
<td>90</td>
<td>&lt; 9</td>
<td>150 / 180</td>
<td></td>
</tr>
<tr>
<td>20NiCrMo13</td>
<td>1490</td>
<td>1080</td>
<td>13</td>
<td>90</td>
<td>95</td>
<td>&lt; 3</td>
<td>150 / 200</td>
</tr>
<tr>
<td>15NiMoCr10</td>
<td>1390</td>
<td>1110</td>
<td>13</td>
<td>90</td>
<td>95</td>
<td>&lt; 3</td>
<td>230 / 280</td>
</tr>
<tr>
<td>31CrMoV9</td>
<td>1080</td>
<td>750</td>
<td>&gt;12</td>
<td>KV=50</td>
<td>97</td>
<td>&lt;3</td>
<td>&gt;580</td>
</tr>
<tr>
<td>33CrMoV12-9</td>
<td>1250</td>
<td>1050</td>
<td>&gt;16</td>
<td>110</td>
<td>108 / 120</td>
<td>&lt;3</td>
<td>= 600</td>
</tr>
<tr>
<td>32CrMoV5</td>
<td>1250</td>
<td>1150</td>
<td>&gt;15</td>
<td>100</td>
<td>80 / 110</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Rm: Tensile Strength  
Re: Yield Strength at 0.2% Rp0.2  
A: Elongation  
KCU: Impact Energy  
K1C: Toughness  
∆HRC: Hardenability based on Jominy Test, where

\[ ∆HRC = HRC(1.5 mm) - HRC(40 mm) \]

The correction of angle takes account of the deflection and twisting of the rotor as well as the temperature distribution in the teeth over their width and the influence of residual stresses.

The qualitative types of longitudinal corrections are shown in Figures 3a and 3b.

(Note: For steels of low hardenability ∆HRC > 8 (hardness difference between HRC40 and the maximum hardness HRC1.5), the thermal deformation which results from the relief of the residual stresses is to be taken into account. The better the hardenability, the flatter will be the hardness line of the Jominy curve and the lower ∆HRC (see Fig. 4a.).)

Materials

In addition to the standard materials for case hardening and nitriding, Tables 1 and 2 show alternatives that give improvements in fracture toughness and ductility. For case hardening these are the materials 20NiCrMo13, 15NiMoCr10 and AISI 9317, and for achieving greater nitrided depths during nitride hardening, the materials are 32CrMoV13 and 32CrMoV5.

These materials all have good hardening characteristics (∆HRC). The flatter the hardness line of the Jominy curve and the smaller ∆HRC, the greater is the hardenability (Fig 4a).

For case hardening (carburizing) steels with around the same Rm (tensile strength) of 1,300–1,400 MPa, those of low ∆HRC value should be favored, especially for solid parts (Fig. 4b).

To minimize internal stresses, complete through-hardening should be achieved. From the results of the Jominy test, predictions can be made regarding the progression of the hardness curve, i.e. the so-called “U-curve.” (See Figure 4c, based on the example of a round bar of 100 mm.)

Heat Treatment

For high-performance gears, only carburizing or nitriding are considered. The most economic form of heat treatment is undoubtedly case hardening. It allows an almost unlimited range of adjustments to the desired hardness depth and in all standards has the high-
est values for long-term resistance to pitting and tooth flexure.

The advantages and disadvantages of hardening processes are compared in Table 3.

It can be seen from Table 2 that carburizing shows the highest admissible fatigue strength values, and therefore the components are smaller than with nitride hardening. A disadvantage, however, is the high risk of distortion of the components during quenching, which may result in unknown residual stresses.

Nitriding, on the other hand, is a low-distortion hardening method where the whole heat treatment process is made below the transformation temperature. It is unfavorable, however, that only small hardness penetration depths can be obtained, ranging from 0.5–0.6 mm with normal nitriding steels and up to approximately 1.4 mm with special steels. Moreover, it can be seen from Figure 5 that the hardness progression curve in the nitriding process drops very steeply towards the base material. It is therefore indispensable to determine the position of the maximum transverse strain, which is, according to the Hertzian stress theory, below the tooth surface.

In particular with nitriding, but also with carburizing, the transverse strain progression must be checked, and care must be taken that its maximum will be inside the hardened layer.

Figures 6 and 7 show test results of Hertzian stress on a wheel disc and a test gearbox dependent on the ratio

---

**Table 2—Composition or Typical Analysis (%)**

<table>
<thead>
<tr>
<th>Material Class</th>
<th>C</th>
<th>Ni</th>
<th>Cr</th>
<th>Mo</th>
<th>Mn</th>
<th>Si</th>
<th>Cu</th>
<th>V</th>
<th>Main Applications</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>CARBURIZING</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Cr basis—Hardenability ∆HRC &gt; 8/10</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>18CrNiMo7-6</td>
<td>0.14/0.17</td>
<td>1.40/3.75</td>
<td>1.50/0.95</td>
<td>0.25</td>
<td>0.08</td>
<td>nom.</td>
<td>—</td>
<td>—</td>
<td>P &lt; 50 MW</td>
</tr>
<tr>
<td>Ni basis—Hardenability ∆HRC &gt; 8/10</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>14NiCr14</td>
<td>0.12/0.17</td>
<td>3.25/3.75</td>
<td>0.60/0.95</td>
<td>0.15</td>
<td>max</td>
<td>0.40/0.70</td>
<td>0.35 max</td>
<td>—</td>
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</tr>
<tr>
<td>14NiCrMo13-4</td>
<td>0.11/0.17</td>
<td>3.00/0.10</td>
<td>0.80/0.25</td>
<td>0.30/0.60</td>
<td>0.40 max</td>
<td>—</td>
<td>—</td>
<td>USA—critical aerospace gear</td>
<td></td>
</tr>
<tr>
<td>AISI 9310</td>
<td>0.13/0.18</td>
<td>3.00/0.5</td>
<td>1.00/0.15</td>
<td>0.08/0.65</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>USA—critical aerospace gear</td>
<td></td>
</tr>
<tr>
<td>Ni basis—High Hardenability ∆HRC &lt; 8</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>AISI 9317</td>
<td>0.15/0.20</td>
<td>3.00/0.5</td>
<td>1.00/0.15</td>
<td>0.08/0.65</td>
<td>0.20/0.35</td>
<td>—</td>
<td>—</td>
<td>USA—critical aerospace gear</td>
<td></td>
</tr>
</tbody>
</table>

**Table 2—Composition or Typical Analysis (%)**

<table>
<thead>
<tr>
<th>Material Class</th>
<th>C</th>
<th>Ni</th>
<th>Cr</th>
<th>Mo</th>
<th>Mn</th>
<th>Si</th>
<th>Cu</th>
<th>V</th>
<th>Main Applications</th>
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<tbody>
<tr>
<td><strong>NITRIDING</strong></td>
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<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2.5% Cr basis—Very High Hardenability ∆HRC &lt; 2/3—High Toughness</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>31CrMoV9</td>
<td>0.28/0.34</td>
<td>—</td>
<td>2.30/2.70</td>
<td>0.15/0.25</td>
<td>0.40/0.70</td>
<td>—</td>
<td>—</td>
<td>0.10/0.20</td>
<td>P &lt; 40 MW</td>
</tr>
<tr>
<td>33CrMoV12-9</td>
<td>0.29/0.35</td>
<td>—</td>
<td>2.80/3.20</td>
<td>0.80/1.20</td>
<td>&lt;</td>
<td>0.35 &lt;</td>
<td>0.25/0.35</td>
<td>P &gt; 30 MW PowerGen + Mechanical Drive</td>
<td></td>
</tr>
</tbody>
</table>

**Table 2—Composition or Typical Analysis (%)**

<table>
<thead>
<tr>
<th>Material Class</th>
<th>C</th>
<th>Ni</th>
<th>Cr</th>
<th>Mo</th>
<th>Mn</th>
<th>Si</th>
<th>Cu</th>
<th>V</th>
<th>Main Applications</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>CrMo basis—Very High Hardenability ∆HRC &lt; 2/3</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>32CrMoV5</td>
<td>0.32</td>
<td>—</td>
<td>1.40</td>
<td>1.20</td>
<td>—</td>
<td>—</td>
<td>0.30</td>
<td>Deep nitriding</td>
<td></td>
</tr>
</tbody>
</table>

(*) Aubert et Duval and (**) Normes Françaises AMS6481
of the effective hardness penetration depth to the equivalent radius of curvature in the pitch point. In addition, the calculated limiting curves of ISO 6336-5 and API 613 are shown. These tests and experimental values show that the Hertzian stress is a variable which depends on the gearbox size. Figure 7 shows typical speeds and power ranges for nitrided gears.

Nitrided surfaces are harder and show more brittleness in case of shock strains than carburized ones. Also, the damage curve in the fatigue strength for finite life in nitrided gears is very flat in comparison to carburized ones. This factor influences the rating of gears for starting, shock and short-circuit torques. (See Table 3 for factors ZNT and YNT). The fatigue strength values in regard to quality MQ and ME, however, do not much differ from carburizing. The recalculation of a 75 MW gas turbine gearbox shows that in high-performance gearboxes, the residual stresses have much influence on total strain. Mainly in the case of carburizing, the residual stresses can be different. It is the main advantage of nitriding that the inner residual stresses are very low.

**Rating of Shafts**

Experience shows that for gear units with wheels of high volume concentration, an inspection for mechanical fracture properties is indispensable, besides the usual strength hypotheses.

### Shaft Designs

There are various shaft design concepts, which have influences for the rotor vibration and the quality of the gear. The most used designs are:
- Shrink-fit design.
- Pinion and wheel in one-piece design

**Shrink-Fit Design.** The shrink-fit design is the most used shaft/hub connection, as the optimal material can be chosen for shaft and wheel. The shaft is transmitting the torque. Therefore a through-hardened steel with the appropriate strength properties will be used.

The usual materials are 42CrMoV4 and for elevated requirements 26NiCrMoV14-5, 30CrNiMo8, or
35NiCrMo16.

The gearing is hardened, i.e. carburized or nitrided steel.

The most used wheel materials (Table 1) for carburizing are 18CrNiMo7-6, 20NiCrMo13 or 15NiMoCr10. The most used materials for nitriding are 31CrMoV9 and 32CrMoV12-9, 32CrMoV5 or 39CrMoV13-9 for extended nitriding depths.

However, the shrink-fit design is limited by the influence of centrifugal forces, and API 613 as well as ISO 13691 do not accept the shrink-fit design for pitch-line velocities over 150 m/sec. In those cases, the one-piece version must be applied. It should be mentioned here that pinions are always made from one piece.

**Wheel and Shaft in One Piece.** In gear units with transmission powers of 70 MW and more, the one-piece design requires a forging with much weight and much volume concentration, especially in the gearing base area. It is important that such forgings, including pre-turning and ultrasonic testing, are ordered directly from the steel manufacturer.

A specification must be prepared in common, determining all the manufacturing process steps like melting, analysis, ingot size, forging ratio, heat treatment, purity regarding oxides and sulfides, mechanical properties as well as test conditions and acceptance criteria.

Figure 8 shows how the forging should be configured in the gearing area in order to be sure that any flaws or gas bubbles due to blowholes do not exist.

The wheel shaft can be a solid-shaft or hollow-shaft design; due to better hardenability, the hollow-shaft design is preferred. The explanations below show the differences of the two designs with regard to strength behavior.

**Solid Shaft.** In the solid shaft, stresses are lower, as can be seen from Mohr’s circle. Figure 9 shows the stress comparison between solid and hollow shafts, under centrifugal force, of a 75 MW gas turbine gearbox. Figures 10
and 11 show the progression of the individual stresses. To be added are the residual stresses due to heat treatment and thermal stresses due to temperature gradients in the wheel body.

A disadvantage when using solid shafts is the risk of non-metallic inclusions in the core as well as—in the hardening process—the risk of ferrite contents in the structure of the core area (insufficient core hardening) and thus insufficient strength.

**Hollow Shaft.** (See also API 613, 5th Edition, 2.5.3.3.) Here the stresses are higher, as can be seen from Mohr’s circle (Fig. 9), but due to the internal bore, the core problems of the solid shaft are eliminated.

Figure 10 shows the progression of the individual stresses, and Figure 12 shows that also with the multiaxial quotient $q$ according to Clausmeyer, the hollow shaft is less favorable than the solid shaft.

To be added for both shaft designs are the residual stresses after carburizing and thermal stresses due to the temperature gradient in the wheel.

In the solid shaft, these are residual tensile stresses, while in the hollow shaft a shifting to the desired pressure area takes place in the bore surface.

**Calculation Methods.** In this section, the calculation of a shrink fit is left out and assumed to be known.

In particular, gears are concerned in which gearing and shaft are a unit, which means that both parts are made of the same material and remain always together during heat treatment.

The dimensioning of the shaft is made preferably according to the transverse strain hypothesis for bending and torsion:

$$
\sigma_z = \sqrt{\sigma_x^2 + 4\tau^2} < \sigma_{zul}
$$

where

- $\sigma_z$ comparative stress (N/mm²)
- $\sigma_x$ bending stress in x-direction (N/mm²)
- $\tau$ transverse stress (N/mm²)
- $\sigma_{zul}$ yield strength (N/mm²)

The yield strength is applied as admissible stress for failure due to plastic deformation.
Because of possible internal defects in those large forgings, a mechanical fracture assessment must be made.

The following calculation example applies to the bull gear of a gas turbine gearbox with a transmission power of 75 MW and a speed of 3,000 rpm (generator speed).

**Total stress of solid shaft**

\[
\sigma_c + \sigma_{\text{residual}} + \sigma_{\text{thermal}} = \sigma_{\text{total}}
\]

The following calculation example applies to the bull gear of a gas turbine gearbox with a transmission power of 75 MW and a speed of 3,000 rpm (generator speed).

<table>
<thead>
<tr>
<th>Term</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\sigma_c)</td>
<td>72.8 N/mm²</td>
</tr>
<tr>
<td>(\sigma_{\text{residual}})</td>
<td>350 N/mm²</td>
</tr>
<tr>
<td>(\sigma_{\text{thermal}})</td>
<td>156 N/mm²</td>
</tr>
<tr>
<td>(\sigma_{\text{total}})</td>
<td>578.8 N/mm²</td>
</tr>
</tbody>
</table>

where:
- \(\sigma_c\): Centrifugal force stress (solid shaft)
- \(\sigma_{\text{residual}}\): Residual tensile stress (assumed)
- \(\sigma_{\text{thermal}}\): Operating thermal stress (\(\Delta T = 135^\circ\text{C}\))
- \(\sigma_{\text{total}}\): Total stress

This total stress must be subjected to a mechanical fracture assessment. In Equation 1, the admissible stress is determined by means of the fracture toughness of the material and a specified maximum defect size, and it is compared with the existing total stress.

\[
S = K_{IC} / K_I > S_{\min}, \quad S_{\min} = 1.5
\]

\[
\sigma_{\text{zul}} = K_{IC} / \sqrt{\pi x \gamma} / Q
\]

(1)

where:
- \(K_I\): Stress intensity in the component
- \(K_{IC}\): Fracture toughness N/mm² (characteristic value of material)
- \(Q\): Crack shape factor
- \(S\): Actual safety factor
- \(S_{\min}\): Minimum required safety factor
- \(c\): Major radius of the elliptical failure (defect)
- \(\sigma_{\text{zul}}\): Actual stress

The crack shape factor \(Q\) is determined by:

\[
Q = 1 + 1.464 \times (a/c)^{1.65} - 0.212 \times (\sigma/R_p)^2
\]

(2)

where:
- \(\sigma/R_p\): Stress relation (for conservative assessments, a value of 0.9 is used)
- \(a\): Minor radius of the elliptical failure (defect)

The value of actual strain is in between, at 578.8 N/mm². It follows that the material 18CrNiMo7-6 for one-piece gears with much volume concentration is within the limit range.

**Summary and Recommendations**

When looking at the Jominy curves in Figures 4a, 4b and 4c, it can be seen that—with regard to hardenability—there are still other alternatives to 18CrNiMo7-6 which provide higher mechanical material parameters.

For further increased operational safety, nitride hardening can be considered. It offers the advantage that the whole heat treatment process is made below the transformation line, which means no risk of distortion and no risk of high residual stress.

To sum up, one can say that the mastery of such gears requires the following conditions:

- Material with fracture toughness \(K_{IC} \geq 80 \text{ Mpa}^{1/2}\).
- Yield strength \(R_e > 750 \text{ MPa}\).
- Sufficient ductility.
- Structure hardenable to the core.
- Proof of sufficient potential hardness increase adapted to U curve (Intensity of potential hardness increase).
- Low distortion during hardening process.
- Reduction of residual stresses by subsequent machining, e.g., excavation.

![Figure 13—Relationship of actual defect size (WEFG) to KSR (CRR).](image-url)
• Selection of a low-distortion hardening method such as gas nitriding.
• Use of special steels for increased hardness penetration depth when nitriding.
• Requirement: Steel production and forging of the ingot to be in the same factory.
• Material Quality: MQ or better ME.
• Melting: Vacuum degassed or remelting according to ESU.
• Cleanliness: \( P_{\text{max}} = 0.007, S_{\text{max}} = 0.007, K4 = 20 \) (Oxide + Sulfide).
• Forging ratio: \( \geq 3.5 \).
• Grain size: Fine grain, predominantly 5 and finer.
• Heat treatment: Hardening and Tempering.
• Non-destructive testing (see Fig. 14)*: Rough machined and finished, followed by ultrasonic inspection test to enhanced SEP 1923 or ÖNORM 3002–class 2–group B7 surface crack test.
• Test mechanical properties:
  o Optimizing notch value and dilatation.
  o Optimizing Jominy-Curve for high alloy steel—restricted hardenability band (H).
  o \( \Delta HRC = HRC_{1.5} - HRC_{40} < 2–3 \) max.

Fig. 14 shows that the check of the shaft core for inclusions and cracks can be detected only by using special sensors for different sound-angles. An ultrasonic inspection test of radial and axial angles with 0° is not sufficient.

From these requirements, the authors give some advice for the material selection as well as for the hardening method, shown in Figure 15 and Tables 4–7. Such advice only represents ideas for the design of high-energy gear boxes which are based on many years of experience.

Standards:
• AGMA 2101, Fundamental Rating Factors and Calculation Methods for Involute Spur and Helical Gear Teeth.
• AGMA 6011, Specification for High Speed Helical Gear Units.
• ISO/TR 13989–1, Calculation of scuffing load capacity of cylindrical, bevel and hypoid gears, Part 1: Flash temperature method.
• ISO/TR 13989–2, Calculation of scuffing load capacity of cylindrical, bevel and hypoid gears, Part 2: Integral temperature method.
• ISO 6336–5, Calculation of load capacity of spur and helical gears, Part 5: Strength and quality of materials.
• ISO 1328–1, Cylindrical gears—ISO systems of accuracy—Part 1: Definitions and allowable values of deviations relevant to corresponding flanks of gear teeth, 1995.
• SEP 1923, Ultrasonic testing of forgings for higher requirements, in particular for turbines and generators.
• ÖNORM 3002, Ultrasonic testing of steel forgings—Performance inspection coverage, quality level.

References
2. FVA-Programs Research—Reports and Calculation—Programs of the German Gear Manufactures within the FVA (Research Association Gear Technology), available only for members of the FVA.
Table 4—HEC (High Energy Criterion) value.

<table>
<thead>
<tr>
<th>MATERIAL CLASS</th>
<th>HEC (J/cm²)</th>
<th>Fracture Toughness K_{IC} MPa\cdot m^{1/2}</th>
</tr>
</thead>
<tbody>
<tr>
<td>18CrNiMo7-6</td>
<td>&lt; 2,600</td>
<td>78</td>
</tr>
<tr>
<td>20NiCrMo13</td>
<td>2,600–3,700</td>
<td>95</td>
</tr>
<tr>
<td>15NiMoCr10</td>
<td></td>
<td></td>
</tr>
<tr>
<td>32CrMoV12-9</td>
<td>&gt; 3,700</td>
<td>108 / 120</td>
</tr>
<tr>
<td>32CrMoV5</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

HEC (J/cm²) = 0.25*M*V^2 / D*L

M : Mass (kg)                  D : Pitch diameter (m)                       V : Pitchline velocity (m/sec)                   L : Total width plus gap at double helical

Table 5—Bulk operating temperature recommendations.

<table>
<thead>
<tr>
<th>MATERIAL CLASS</th>
<th>θ_{Tooth Operating} (°C)</th>
<th>θ_{BULK} (°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td>18CrNiMo7-6</td>
<td>150 / 180</td>
<td>&lt; 180</td>
</tr>
<tr>
<td>20NiCrMo13</td>
<td>180 / 200</td>
<td>&lt; 200</td>
</tr>
<tr>
<td>15NiMoCr10</td>
<td>240 / 260</td>
<td>&lt; 260</td>
</tr>
<tr>
<td>32CrMoV12-9</td>
<td>&gt; 600</td>
<td>&lt; 300</td>
</tr>
<tr>
<td>32CrMoV5</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Tooth Operating Temperature @ Material Tempering Temp.

θ_{MESH OIL SIDE EJECTION} = 0.4 * V_{t} + θ_{OIL INLET} (°C)

θ_{BULK} = 1.72 * θ_{MESH OIL SIDE EJECTION} * A * B

A = 0.92  m_{n} = 6  B = 0.73
A = 0.96  m_{n} = 8  B = 0.87
A = 1.00  m_{n} = 10 B = 1.00
A = 1.04  m_{n} = 12 B = 1.13
A = 1.08  m_{n} = 14 B = 1.27

for single helical L or F_{w} : < 600  β = 7–15°

for double helical L or F_{w} : < 2 x 550  β = 25–30°

σ_{H}^{A} m_{n} B

550  0.92  6  0.73
575  0.96  8  0.87
600  1.00  10 B = 1.00
625  1.04  12 B = 1.13
650  1.08  14 B = 1.27

Table 6—Forging, material class recommendations (Use with Figure 14).

<table>
<thead>
<tr>
<th>SHAFT/BLANK CONSTRUCTION</th>
<th>Pinion</th>
<th>Gear</th>
</tr>
</thead>
<tbody>
<tr>
<td>MATERIAL CLASS</td>
<td>Bar or Forging</td>
<td>Forging</td>
</tr>
<tr>
<td>BAR 1 L/D&gt;8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>18CrNiMo6-7</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>20NiCrMo13</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>15NiMoCr10</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>32CrMoV12-9</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>32CrMoV5</td>
<td>Yes</td>
<td>Yes</td>
</tr>
</tbody>
</table>

: Hardenability (Residual stresses)
Erwin Dehner is the former managing director of BHS Cincinnati, where he was employed for more than 30 years. He also spent 30 years as a member of the advisory group of the FVA (union for research and gear development within the VDMA). He served as convener of the ISO working group WG11 “High-Speed Enclosed Gear Drives” from 1993–2001. That group’s work resulted in the ISO standard 13691. Dehner also served from 1995–2001 as a discussion leader at the Turbomachinery symposium held each year in Houston. He has written for numerous publications about ships, turbogears and bearings, mainly in German. Although retired since 2001, he has since then served as a consultant and as an instructor in a seminar for epicyclic gears at the Technische Akademie Esslingen.

François Weber is a former member of the board of management of Flender-Graffenstaden, where he worked for 40 years. Prior to serving on the board, he was managing director for sales and design. He has served for 20 years as a member in the advisory group “Gear Development” of UNITRAM (the Association of French Manufacturers of Mechanical Power Transmissions), and he has also served on committees and working groups of national and international standards bodies. He has written for numerous publications about design, material selection and best practices for turbo-load gears and steam turbines. Since retiring in 1999, he has worked as a consultant on turbogear problems.

### Table 7—Power, pitchline velocity recommendations.

<table>
<thead>
<tr>
<th>MATERIAL CLASS</th>
<th>RATINGS</th>
<th>APPLICATIONS</th>
</tr>
</thead>
<tbody>
<tr>
<td>18CrNiMo6-7</td>
<td>35 / 50</td>
<td>Conventional Turbogears</td>
</tr>
<tr>
<td>20NiCrMo13</td>
<td>40 / 100</td>
<td>High hardenability, high core hardness and high fatigue strength, ideally suited for critical High Energy Turbogears.</td>
</tr>
<tr>
<td>15NiMoCr10</td>
<td>40 / 100</td>
<td>Combination of high-temperature performance, deep hardenability, good core properties and high fatigue resistance, ideally suited for very critical High Energy Turbogears.</td>
</tr>
<tr>
<td>32CrMoV12-9</td>
<td>&gt; 30</td>
<td>Combination of high-temperature performance, high strength, high toughness and fatigue resistance of the core. Furthermore very deep cases with high compressive residual stresses. Suited for High Energy Turbogears with severe loading in terms of service temperature or lubrication.</td>
</tr>
<tr>
<td>32CrMoV5</td>
<td>&gt; 30</td>
<td>Similar to 32CrMoV13 with reduction of the duration and the cost of nitriding.</td>
</tr>
</tbody>
</table>

3. Tables for Material and Selection Lists, Support by Aubert & Duval, Buderus.
13. Joly, P. “A Carburizing steel with improved properties for highly stressed gears, a higher temperature carburizing steel,” private communication, authorized by the author.
14. Joly, P. and Daniel Girordin. “Deep Nitriding of the 32CrMoV13 Steel (AMS 6481 0.32 % C - 3 % Cr - 1 % Mo - 0.2 % V) and its Application for Aerospace Bearings,” Toronto, May 2005. Private communication, authorized by the authors.